

Quarter 1

Quarter 1	Quarter 2	Quarter 3	Quarter 4
Linear Programming, Organizing and Interpreting Data, Data Descriptions	Probability and Counting Rules, Probability Distributions	Normal Probability Distribution, Confidence Intervals, Financial Mathematics	Financial Mathematics (cont.), Logic, Boolean Algebra
August 12, 2019 – October 11, 2019	October 21, 2019 – December 20, 2019	January 6, 2020 – March 13, 2020	March 23, 2020 – May 22, 2020
AM.A.LP.A.1	AM.D.CR.A.1	AM.D.ND.A.1	AM.G.L.A.1
AM.A.LP.A.2	AM.D.CR.A.2	AM.D.ND.A.2	AM.G.L.A.2
AM.A.LP.B.3	AM.D.CR.A.3	AM.D.CI.A.1	AM.G.L.A.3
AM.A.LP.B.4	AM.D.CR.A.4	AM.D.CI.A.2	AM.G.L.A.4
AM.D.ID.A.1	AM.D.CR.A.5	AM.D.CI.A.3	AM.G.L.B.5
AM.D.ID.A.2	AM.D.CR.B.7	AM. A. PS. A.1	AM.G.L.B.6
AM.D.ID.A.3	AM.D.CR.B.8	AM.N.NQ.A.1	AM.G.L.B.7
AM.D.ID.A.4	AM.D.CR.B.9	AM.N.NQ.A.2	AM.G.L.B.8
AM. A. PS. A.1	AM.D.CR.B.10	AM.N.NQ.A.3	AM.A.LB.A.1
AM.D.CR.B.10	AM.D.ID.A.4	AM.N.NQ.A.4	AM.A.LB.A.2
	AM.D.ID.A.5	AM.N.NQ.B.5	AM.A.LB.B.3
	AM.D.ID.A.6	AM.N.NQ.B.6	AM.A.LB.B.4
	AM.D.ID.A.7	AM.N.NQ.B.7	AM.N.NQ.C.9
	AM. A. PS. A.1	AM.N.NQ.B.8	AM.N.NQ.C.10
		AM.N.NQ.C.9	AM.D.CI.A.1
		AM.N.NQ.C.10	AM.D.CI.A.2
			AM.D.CI.A.3
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Applied Mathematical Concepts

Introduction

Destination 2025, Shelby County Schools' 10-year strategic plan, is designed not only to improve the quality of public education, but also to create a more knowledgeable, productive workforce and ultimately benefit our entire community.

What will success look like?



In order to achieve these ambitious goals, we must collectively work to provide our students with high quality, college and career ready aligned instruction. The Tennessee State Standards provide a common set of expectations for what students will know and be able to do at the end of a grade. The State of Tennessee provides two sets of standards, which include the Standards for Mathematical Content and The Standards for Mathematical Practice. The Content Standards set high expectations for all students to ensure that Tennessee graduates are prepared to meet the rigorous demands of mathematical understanding for college and career. The eight Standards for Mathematical Practice describe the varieties of expertise, habits of mind, and productive dispositions that educators seek to develop in all students. The Tennessee State Standards also represent three fundamental shifts in mathematics instruction: focus, coherence and rigor.

Instructional Shifts for Mathematics



Throughout this curriculum map, you will see resources as well as links to tasks that will support you in ensuring that students are able to reach the demands of the standards in your classroom. In addition to the resources embedded in the map, there are some high-leverage resources around the content standards and mathematical practice standards that teachers should consistently access. For a full description of each, click on the links below.



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How to Use the Maps

Overview

An overview is provided for each quarter and includes the topics, focus standards, intended rigor of the standards and foundational skills needed for success of those standards.

Your curriculum map contains four columns that each highlight specific instructional components. Use the details below as a guide for information included in each column.

Tennessee State Standards

TN State Standards are located in the left column. Each content standard is identified as Major Content or Supporting Content (for Algebra I, Algebra II & Geometry only). A key can be found at the bottom of the map.

Content

This section contains learning objectives based upon the TN State Standards. Best practices tell us that clearly communicating measurable objectives lead to greater student understanding. Additionally, essential questions are provided to guide student exploration and inquiry.

Instructional Support & Resources

District and web-based resources have been provided in the Instructional Support & Resources columns. You will find a variety of instructional resources that align with the content standards. The additional resources provided should be used as needed for content support and scaffolding. The inclusion of vocabulary serves as a resource for teacher planning and for building a common language across K-12 mathematics. One of the goals for Tennessee State Standards is to create a common language, and the expectation is that teachers will embed this language throughout their daily lessons.

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Topics Addressed in Quarter

- Linear Programming
- Organizing and Interpreting Data
- Data Descriptions

Overview

During quarter one students review solving systems of equations and inequalities using various methods including substitution, elimination, and matrices. Students are then introduced to applications of solving linear equations and inequalities. In particular, students use linear programming, a method for solving problems in which a particular quantity must be maximized or minimized based upon other constraints. Students solve problems using linear programming, a widely used tool in management science/business.

Students have encountered some statistics and probability in previous courses, however in this quarter students build upon previous standards by organizing and exploring data and making inferences and justifying conclusions. Students extend their work in statistics by applying statistics ideas to real-world situations. They link classroom mathematics and statistics to everyday life, work, and decision-making, by modeling real-world situations. They choose and use appropriate mathematics and statistics to analyze situations, to understand them better, and to improve decisions. Students distinguish between population and sample, parameter and statistic, and descriptive and inferential statistics; recognizing purpose and difference of sample surveys, experiments, and observational studies; interpreting differences in shape, center, and spread including effects of outliers and using shape, center, and spread of comparable data to decide on appropriate statistical measures. Student also graph and interpret quantitative data sets using a variety of graphs.

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TN STATE STANDARDS	CONTENT	CONTENT INSTRUCTIONAL SUPPORT & RESOURCES	
Systems of Equations and Inequalities Linear Programming			
(Review – Algebra 2)* Domain: Reasoning with Equations and Inequalities Cluster: Solve systems of equations and nonlinear inequalities *A2.A.REI.C.4 Write and solve a system of linear equations in context.	 (Allow approximately 5 weeks for it is a system of equations and inequalities and how can they be used to model real-life situations? How can a system of equations or inequalities be solved algebraically and graphically? What does it mean to look for a solution(s) of a system of equations or inequalities? Objective(s): Students will: verify ordered pair solutions solve linear systems by graphing solve linear systems by substitution solve linear systems by elimination recognize inconsistent systems and dependent systems use a system of equations to model and solve applications visualize a solution in three dimensions check ordered triple solutions solve linear systems in three variables recognize inconsistent and dependent systems 	Adv. Alg. & Trig. Textbooks 8.1 Linear Systems in Two Variables with Applications (Coburn) 8.2 Linear Systems in Three Variables with Applications (Coburn) 8.1 Systems of Linear Equations in Two Variables (Blitzer) 8.2 Systems of Linear Equations in Three Variables (Blitzer) Tennessee Finite Math (Maki & Thompson) 5.1 Review of Equations and Graphs of Lines Calculator Exercises: Graph of a Linear Equation, p.154; Find Linear Models, p.158 5.2 Formulation and Solution of Systems of Linear Equations in Two Variables Calculator Exercise; Graph and Solve a System of Equations, p.170 5.3 Formulation and Solution of Systems of Linear Equations in Three or More Variables Math Lab: Use the Echelon Method to Solve Systems of Equations Calculator Exercise: Reduce and Augmented Matrix, p.194 Additional Resources: <u>Advanced Mathematical Concepts</u> <u>2.1 Solving Systems of Equations in Two Variables</u> <u>2.2 Solving Systems of Equations in</u> <u>Three Variables</u> <u>1.3 Graphing Linear Equations</u>	 Vocabulary/ Important Terms and Concepts system of equations, simultaneous equations, standard form of a line, y-intercept, slope form, point of intersection, infinitely many solutions, no solution, solution set, parallel lines, perpendicular lines, linear system, solve by substitution, solve by elimination Tennessee Finite Math (Maki & Thompson) Algorithm for solving a system of linear equations, augmented matrix, coefficient matrix, consistent system, coordinates in the plane and in three- dimensional space, echelon method, equation of a plane, function, function notation, Gaussian elimination, Gauss-Jordan elimination, general equation of a line, inconsistent system, intercept, line, linear extrapolation, linear interpolation, linear model, reduced row-echelon form, reduction method, row-echelon form, slope, slope-intercept equation of a line, solution of a system of linear equations, substitution method, system of linear equations, substitution method, system of linear equations, theorem on the solution set of a system of linear equations Section Exercise Sets, pp.160-161; 172-174; 195-196 Chapter Exercises, pp.197-199 Writing in Math/Discussion What is a system of linear equations? Provide an example with your description.



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TN STATE STANDARDS	CONTENT	INSTRUCTIONAL SUP	PORT & RESOURCES
		<u>1.6 Real-world Data with Linear</u> <u>Functions</u> <u>Khan Academy: Systems of Equations</u> <u>Khan Academy: Systems of Inequalities</u> <u>Khan Academy: Systems of Inequalities</u> <u>Khan Academy: Systems of Inequalities</u> Task(s) <u>Mathematics Vision Project; Module 1-</u> <u>Systems of Equations & Inequalities</u> (Choose from the twelve tasks) <u>Supply and Demand</u> <u>Systems of Equations & Inequalities Problems</u> <u>Battleships & Mines Lab Activity</u> <u>Cell Phone Problem</u> <u>Road Rage Activity</u> <u>Poster Questions</u> <u>System of Equations Word Problems Wkst</u> <u>System of Equations Wkst</u> <u>System of Systems of linear equations, with an emphasis</u> on the graphical, numerical, and algebraic meaning of the solutions to those systems)	When is it easier to use the addition method rather than the substitution method to solve a system of equations? When using the addition or substitution method, how can you tell if a system of linear equations has no solution? What are some of the real life applications of two-variable linear systems?
(Review – Algebra 2)* Domain: Reasoning with Equations and Inequalities Cluster: Solve systems of equations and nonlinear inequalities <u>*A2.A.REI.C.4</u> Write and solve a system of linear equations in context.	 Essential Question(s): How would you apply what you have learned in systems of inequalities to linear programming? What are some real-world situations that can be solved using linear programming? Objective(s): 	Adv. Alg. & Trig. Textbooks 8.4 Systems of Inequalities and Linear Programming (Coburn) 8.5 Systems of Inequalities (Blitzer) 8.6 Linear Programming (Blitzer) Tennessee Finite Math Textbook 7-1 Formulation of Linear Programming Problems	Vocabulary Bounded (unbounded) set, constraint, corner point, decision variables, feasible set, graphical solution method for linear programming problems, linear programming problem, objective function, optimization problem, solution method for linear programming problems, theorem on solutions



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IN STATE STANDARDS	CONTENT		PORT & RESOURCES
Domain: Linear Programming	Students will:	7-3 Graphical Solution of Linear Programming	of linear programming problems, vertex of
Cluster: Use linear programming techniques to solve real-world problems	solve a linear inequality in two variables		Tennessee Finite Math Textbook
AM.A.LP.A.1 Use mathematical models	• solve a system of linear inequalities	Topposson Finite Math (Maki & Thompson)	Bounded (unbounded) set, constraint, corner point,
involving equations and systems of	 solve applications using a system of linear inequalities 	7 1 Formulation of Linear Programming	decision variables, feasible set, graphical solution
equations to represent, interpret, and analyze	 solve applications using linear 	Problems	programming problem, objective function,
various contexts, and other real-world	programming	7.2 Systems of Linear Inequalities in Two	optimization problem, solution method for linear
phenomena.	• represent, interpret, analyze, and model	Variables	linear programming problems, theorem on solutions of
programming problems graphically	linear programming problems	Calculator Exercise: Explore Systems of Inequalities, p.254	region
and by computational methods.		7.3 Graphical Solution of Linear Programming	Writing in Math/Discussion
		Problems in Two Variables	Explain how to graph $2x - 3y < 6$.
Domain: Linear Programming		Additional Resource(s)	
problems.		Advanced Mathematical Concepts	What does it mean if a system of linear
<u>AM.A.LP.B.3</u> Use linear programming to solve		2.6 Solving Systems of Linear Inequalities 2.7 Linear Programming	
AM.A.LP.B.4 Interpret the meaning of the		engage ^{ny} : Systems of Inequalities Lesson 17	What kinds of problems are solved using the
maximum or minimum value in terms of the		Khan Academy: Modeling with Systems of Inequalities	linear programming method?
objective function.		Math Vision Project: Systems of Equations	In your own words, describe what a linear
		and Inequalities pp.123-131	programming problem is and how it can be solved.
		FiniteHelp Lecture Video- 7.1	
		FiniteHelp Practice Problems Ch. 7	
		Linear Programming Problem Video Part 1	
		Linear Programming Problem Video Part 2	
		Linear Programming Linear Programming (Chapter 2)	



TN STATE STANDARDS	CONTENT	INSTRUCTIONAL SUP	PORT & RESOURCES
		Linear Programming Problems <u>A Course In Graphic Design</u> <u>Building Lego Furniture</u> <u>Christmas Tree Class Project</u> <u>Comparing Pay Structures</u> <u>High Step Shoes</u> <u>Helping Hurricane Victims</u> <u>Key Club</u> <u>Pump Up</u>	
	Organizing and	Interpreting Data;	
	(Allow approximately 4 weeks for ir	istruction, review, and assessment)	
 Domain: Organize and Interpret Data Cluster: Analyze data from multiple viewpoints and perspectives. AM.D.ID.A.1 Organize data for problem solving. AM.D.ID.A.2. Use a variety of counting methods to organize information, determine probabilities, and solve problems. AM.D.ID.A.3 Translate from one representation of data to another, e.g., a bar graph to a circle graph. 	 Essential Question(s): How can the study of Statistics be used in real life scenarios? What are the benefits of interpreting data? How do we study data? Objective(s) The student will: Demonstrate knowledge of statistical terms. 	Elementary Statistics Textbook (Bluman) 1-1 Descriptive and Inferential Statistics 1-2 Variables and Types of Data 1-3 Data Collection and Sampling Techniques 1-4 Observational and Experimental Studies 1-5 Uses and Misuses of Statistics Additional Resource(s) Against All Odds Video, Unit 1 What is Statistics?	Vocabulary (Chapter 1) cluster sample, confounding variable, continuous variables, control group, convenience sample data, data set, data value or datum, dependent variable, descriptive statistics, discrete variables experimental study, explanatory variable Hawthorne effect, hypothesis testing, independent variable, inferential statistics interval level of measurement, measurement scales, nominal level of measurement observational study ordinal level of
 AM.D.ID.A.4 Calculate and interpret statistical problems using measures of central tendency and graphs. Domain: Problem Solving Cluster: Apply problem solving techniques to real-world situations. AM.A. PS.A.1 Apply problem solving strategies to real-world situations. <i>Strategies include, but are not limited to: making orderly lists or tables, drawing diagrams, considering simpler problems, looking for patterns, working</i> 	 Differentiate between the two branches of statistics. Identify the measurement level for each variable. Demonstrate knowledge of the four basic sampling methods. Explain the difference between an observational study and an experimental study. Describe the role of randomization in surveys and experiments. 	(Against All Odds is a Video Series that introduces a statistical topic and illustrates it with a real-world example. There is a Student Guide that provides guiding questions as students view the video.) Stat Trek Stats Modeling the World Part I – Exploring & Understanding Data (Chapters 1- 6) Khan Academy Videos Statistics overview Categorical data displays Two-way tables for categorical data	measurement, outcome variable, population, probability, qualitative variables, quantitative variables, quasi-experimental study, random sample, random variable, ratio level of measurement, sample, statistics, stratified sample, systematic sample, treatment group, variable <u>Elementary Statistics Textbook (Bluman)</u> <i>Statistics Today,</i> pp. 2, 29 <i>Critical Thinking Challenges</i> , p. 31 <i>Speaking of Statistics,</i> p. 11



TN STATE STANDARDS	CONTENT	INSTRUCTIONAL SUF	PORT & RESOURCES
backwards, guess and check, using logical reasoning, etc. Domain : Counting and Combinatorial Reasoning	 Recognize faulty questions on a survey and other factors that can bias responses. Know the characteristics of well-designed studies. 	Tasks Interpreting Quantitative & Categorical Data	Applying the Concepts, pp. 13, 16 Extending the Concepts, p.28 Data Projects, p.32 TI-83/84 Step by Step, pp. 21-22
Cluster: Use combinatorial reasoning to solve real-world problems.	 Explain how statistics can be used and misused. 		
AM.D.CR.B.10 Analyze decisions and strategies using probability concepts (e.g., product testing, medical testing, pulling a hockey goalie at the end of a game).	 Essential Question(s): How do you construct a frequency distribution? How can frequency tables help us to find trends in real life scenarios? How do you use and interpret stem and leaf plots? How do you represent data in frequency distributions using histograms, frequency polygons, and ogives? Objective(s): The student will: Organize univariate data using a frequency distribution. Represent quantitative data graphically using histograms, dot plots, and orgives. Represent data using bar graphs, Pareto charts, time series graphs, and pie graphs. Draw and interpret a stem and leaf plot. 	Elementary Statistics Textbook (Bluman) 2-1 Organizing Data 2-2 Histograms, Frequency Polygons, and Orgives 2-3 Other Types of Graphs Additional Resource(s) Against All Odds Video, Unit 3 Histograms Against All Odds Video, Unit 5 Boxplots Against All Odds Video, Unit 10 Scatterplots (Against All Odds video, Unit 10 Scatterplots (Against All Odds is a Video Series that introduces a statistical topic and illustrates it with a real-world example. There is a Student Guide that has guiding questions as students view the video.) Stat Trek Stats Modeling the World Part II – Exploring Relationships Between Variables (Chapters 7- 10) Khan Academy Videos <u>Histograms</u> <u>Comparing features of distributions</u> Stem-and-leaf plots	Vocabulary (Chapter 2): bar graph, categorical frequency distribution, class, class boundaries, class midpoint, class width, cumulative frequency, cumulative frequency distribution, frequency, frequency distribution, frequency polygon, grouped frequency distribution, histogram, lower class limit, ogive, open-ended distribution, Pareto chart, pie graph, raw data, relative frequency graph, stem and leaf plot, time series graph, ungrouped frequency distribution, upper class limit <u>Elementary Statistics Textbook (Bluman)</u> <i>Statistics Today</i> , pp. 36, 97 <i>Critical Thinking Challenges</i> , pp.99-100 <i>Speaking of Statistics</i> , pp.74, 81 <i>Applying the Concepts</i> , pp. 45-46, 60, 83-84 <i>Extending the Concepts</i> , pp. 48, 63, 86-87 <i>Data Projects</i> , pp.100-101 <i>TI-83/84 Step by Step</i> , pp. 64-65, 91
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TN STATE STANDARDS	CONTENT	INSTRUCTIONAL SUP	PORT & RESOURCES
	From the Donothing ()	Line graphs Box and whisker plots Task(s) Texting By the Numbers- A Solidify Understanding Task, pp. 3-7 Accuracy of Carbon 14 Dating I Haircut Costs Speed Trap Other Illustrative Statistics & Probability Tasks	Neghology (Objector 2)
 Domain: Organize and Interpret Data Cluster: Analyze data from multiple viewpoints and perspectives. AM.D.ID.A.1 Organize data for problem solving. AM.D.ID.A.2. Use a variety of counting methods to organize information, determine probabilities, and solve problems. AM.D.ID.A.3 Translate from one representation of data to another, e.g., a bar graph to a circle graph. AM.D.ID.A.4 Calculate and interpret statistical problems using measures of central tendency and graphs. 	 Essential Question(s): How do we organize, display, and describe data? How does mean, median, and mode describe data? How can percentiles be used when comparing an individual to the norm? How does exploratory data analysis help us to better understand our data? Objective(s): The student will: Use a variety of numerical techniques to describe the central tendency of a distribution including 	Elementary Statistics Textbook (Bluman) 3-1 Measures of Center 3-2 Measures of Variation 3-3 Measures of Position 3-4 Exploratory Data Analysis Additional Resource(s) Against All Odds Video, Unit 4 Measures of Center Against All Odds Video, Unit 6 Standard Deviation	Vocabulary: (Chapter 3) bimodal, boxplot, Chebyshev's theorem, coefficient of variation, data array, decile, empirical rule, exploratory data, analysis (EDA), five-number summary, interquartile range (IQR), mean, median, midrange, modal class, mode, multimodal, negatively skewed or leftskewed distribution, outlier, parameter, percentile, positively skewed or rightskewed distribution, quartile range, range rule of thumb, resistant statistic, standard deviation, statistic, symmetric distribution, unimodal, variance, weighted mean, <i>z</i> score or standard score
 Domain: Normal Probability distribution Cluster: Work with the normal distribution in real-world situations. AM.D.ND.A.1 Calculate the mean (expected value) and standard deviation of both a random variable and a linear transformation of a random variable. 	 mean, median, mode, and midrange Use a variety of numerical techniques to describe the variation in a distribution. These should include variance, standard deviation, and range. Identify the position of a data set using various measures of position. These 	Stats Modeling the World Part III – Gathering Data (Chapters 11-13) Stat Trek Khan Academy Videos Measures of Central Tendency Variance and Standard Deviation Mean and median: The basics More on mean and median	Elementary Statistics Textbook (Bluman) Statistics Today, pp. 104, 175 Critical Thinking Challenges, pp.178-180 Speaking of Statistics, p.109 Applying the Concepts, pp. 118, 137, 166 Extending the Concepts, pp. 121-122, 140- 141, 168 Data Projects, pp.179-180



TN STATE STANDARDS	CONTENT	INSTRUCTIONAL SUP	PORT & RESOURCES
Domain: Problem Solving Cluster: Apply problem solving techniques to real-world situations. AM.A. PS.A.1 Apply problem solving strategies to real-world situations. <i>Strategies</i> <i>include, but are not limited to: making orderly</i> <i>lists or tables, drawing diagrams, considering</i> <i>simpler problems, looking for patterns, working</i> <i>backwards, guess and check, using logical</i> <i>reasoning, etc.</i>	 should include z-scores, percentiles, and interquartile range. Interpret graphical displays in terms of shape, center, and spread of the distribution, as well as gaps and outliers. Use the techniques of exploratory data analysis, including boxplots and five-number summaries, to discover various aspects of data. 	Range, Interquartile range (IQR), Mean absolute deviation (MAD) Population variance and standard deviation Sample variance and standard deviation Sample variance and standard deviation Task(s) Measuring Variability in a Data Set Pick a Pocket Are Female Hurricanes Deadlier than Male Hurricanes? Understanding Standard Deviation Data Distributions – A Solidify/Practice Understanding Task Describing Data Sets with Outliers Yankees vs Mets Other Illustrative Statistics & Probability Tasks	<i>TI-83/84 Step by Step</i> , pp. 158-159, 169-170



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RESOURCE TOOLKIT			
Textbook Resources	Standards	Videos	
	Common Core Standards - Mathematics	Khan Academy	
Advanced Algebra & Trigonometry (Coburn)	Common Core Standards - Mathematics Appendix A	Illuminations (NCTM)	
	http://www.cosstoolbox.org/	Discovery Education	
Algebra & Trigonometry (Blitzer)	<u>Intp://www.ccsstoolbox.org/</u>	The Futures Channel	
	Common Core Lessons	The Teaching Channel	
Advanced Mathematical Concepts	Tennessee Mathematics Standards	<u>Teachertube.com</u>	
		FiniteHelp Lecture Videos	
Elementary Statistics Textbook (Bluman)		Against All Odds Videos (with Study Guides) (A Video Series that	
		example)	
Stats Modeling the World		overipio,	
Tennessee Finite Math (Maki & Thompson)			
Calculator	Interactive Manipulatives	Additional Sites	
Texas Instruments Education	<u>Stat Trek</u>	MathBits (scroll down for Statistics 1 & 2)	
<u>TI-Nspired</u>	Rossmanchance.com	NCTM Math Illuminations	
<u>TICommonCore.com</u>	ACT & SAT	Wolfram Math World	
http://www.casioeducation.com/educators	TN ACT Information & Resources	STatistics Education Web	
Desmos	ACT College & Career Readiness Mathematics Standards	<u>Stat Trek</u>	
	SAT Connections	http://www.edutoolbox.org/tntools (formerly tncore.org)	
SEL Resources	SAT Practice from Khan Academy		
SEL Core Competencies			
The Collaborative for Academic, Social, and Emotional			
Learning (CASEL)			



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